ANNOUNCEMENTS

- MIDTERN: 03/13, wednesday

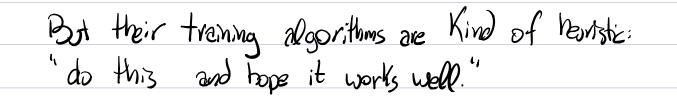
materal: - Decision Trees - KNNS - Perception - Practical issues ( anarfitting , ... - heduction, - Linear models (but not Vernel methods) - in other words, today and wednesday's ledure, bit not 03/11's ledure -Becare I'm behind, no A35 (study for the midtern!)

- Pext lecture:

- Gradient Descent - heading: Why momentum really works, up to Polynomial Regression

LINEAR MODELS

We have so far learned about the perception, decision trees, and K-NN. We studied algorithms to train those makels, and hav to assess ther Delformance.



Here's a different idea: write a formula for bas bad a model is, then "training" means "find the model that optimizes that formula."

Linear models all work by having the training proceedure pick one hyperplane and the formula always gos through the margin that training examples attam.

(We assume all input points have a column with value 1, so no bias term is needed)

Loss-of-model( $\omega$ ) =  $\sum_{(x,y)} loss-of-sample(marajn(x, <math>\omega$ ),  $\gamma$ )

## WHICH LOSS TO CHOOSE?

Misclassification loss: l(m, y) = 0 if sign (m) = y1, otherwise

This is the obvious loss, but we rarely use it, becase it leads to an NP-Hard optimization problem.

To explain what causes the trable, let's refactor our loss definition, so that the loss takes a single parameter, which is "positive on the correct side of the margin".

Our moroin calculation then needs to Know about the label:

margh  $(\omega, x, y) = \langle \omega, x \rangle y$ 

misclassification loss is now And our

 $l_{o}(m) = \begin{cases} 1, & \text{if } m < 0 \\ 0, & \text{otherwise} \end{cases}$ 

CONVEX LOSS SUBPOGATES

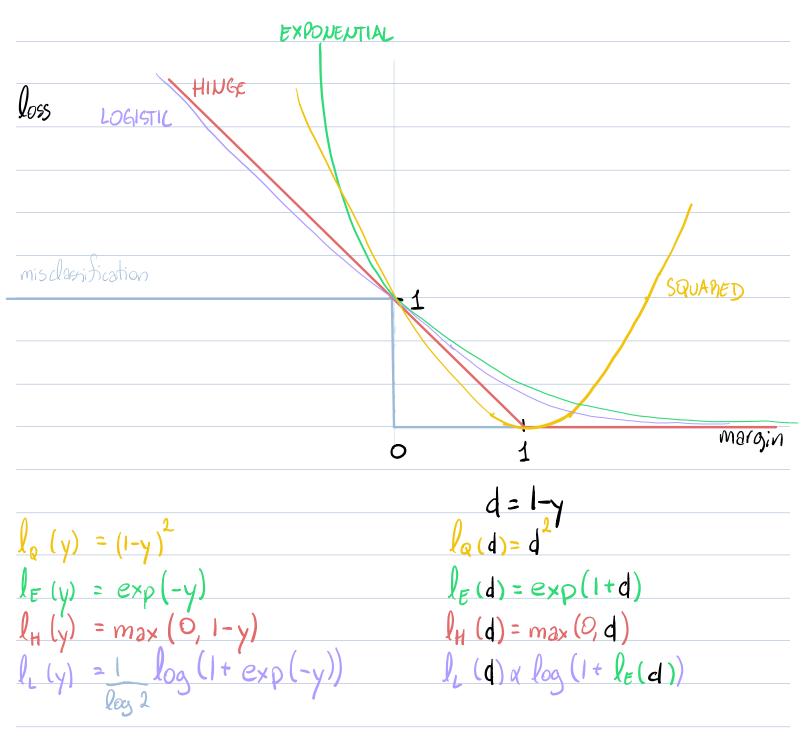
The trade with micdassi tication loss is now graphically clearer. This loss is not convex: loss misclessification 1

Margin

Non-convex optimization is hard to do well. (We will see it later in the course: neural networks are the canonical modern non-convex, non-linear models)

We need losses that are similar to misclassification so that they are useful, but that are also convex (and differentiable) so that they are practical.

## THE CONVEX LOSS 200



QUADRATIC:	Keep it	above zero and easy to got closed form
EXPONENTIAL :	Keep it	monotonic
HINGE :	Keep it	monotonic, compact support on good' side
LO GISTIC:	Keep it	monotonic, smooth, "not too angry"

EMPIPICAL PIKK VS. STRUCTUBAL RISK

What happens with the best model we Sand on training data? On fiture data?

Our loss needs to prevent overfitting. One way to think about the potential for overfitting is by considering how jiggly our model is w.r.t. the training data.

Let's control how flexible or models can be Loss-of-model  $(w) = \sum_{(x,y)} loss-of-sample (y, marajin (x, w, y))$ 

+  $\lambda \cdot \text{model} \cdot \text{complexity}(\omega)$  $\lambda \cdot \| \omega \|^2$ 

If  $w = (0, \dots, 0)$ , has flexible is that model? What if  $w = (10^{100}, \dots, 10^{100})$ ? Use norm of vector 25 proxy for complexity!

THE BEGULARIZATION 200

 $\nabla_{u} \| w \|^{2} = 2 w$ 

le regularization l regularization l, regularization  $l_{0}(\omega) = \sum_{i} [\omega; \neq 0]$ Ľ Le lz regularization lo reau larization  $\|\omega\|_{p} = \sqrt{2|\omega_{i}|^{p}}$ 



